

# Detection and Characterization of Chemical Vapor Fugitive Emissions from Hyperspectral Infrared Imagery by Nonlinear Optimal Estimation

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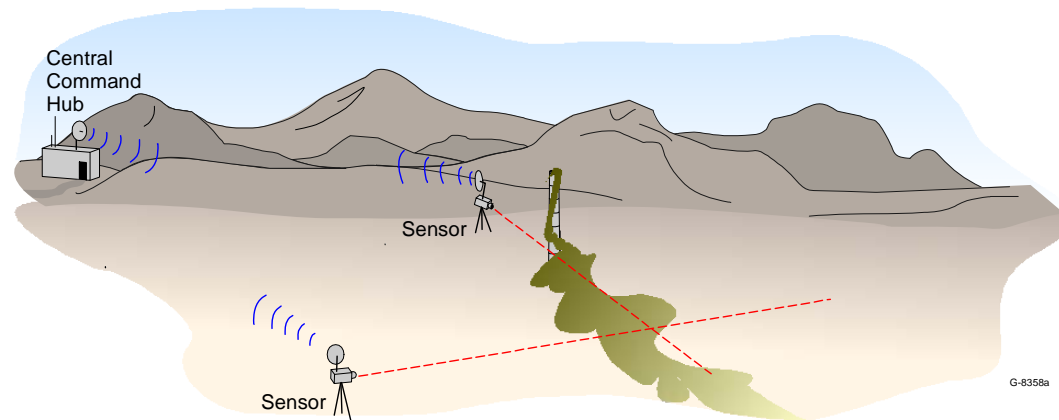
# Agenda

VG10-076-1

- ***Introduction***
- **Nonlinear estimation**
  - Algorithm formulation
  - Test data
  - Results
- **Conclusions**

# Algorithm Development: Overview

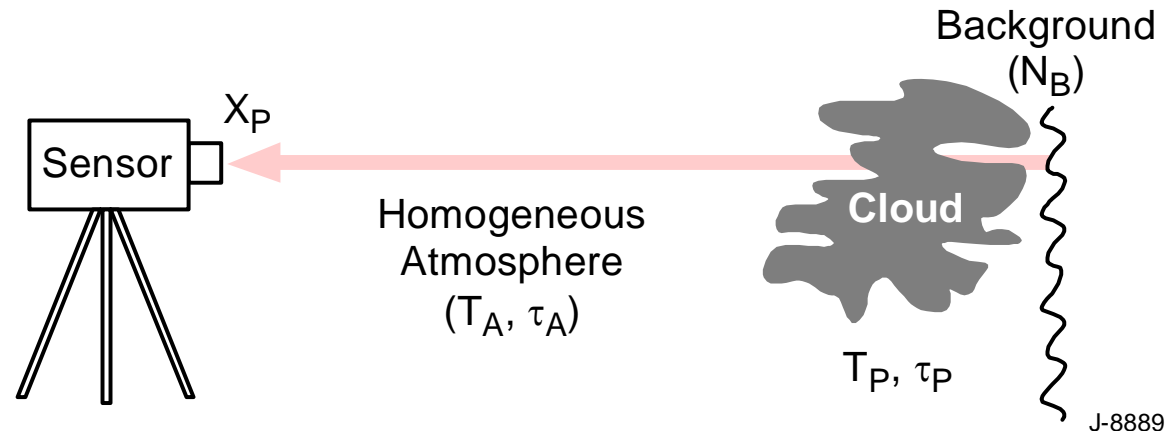
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- **Objectives**
  - Improve pixel-level detection: Reduce probability of false alarm for given  $P_d$
  - Address optically-thick plumes: Improve accuracy of estimated path integrated concentration (column density, CL)
  - Compatible with real-time processing
- **Limitations of current practice**
  - Matched-filter-based detection presumes optically-thin plume
  - Other approaches require prior measurements of background – not compatible with on-the-move detection
- ***Payoff: Improve detection immediately following large-scale release, low-lying plumes; improve mass estimate***

# Problem Formulation

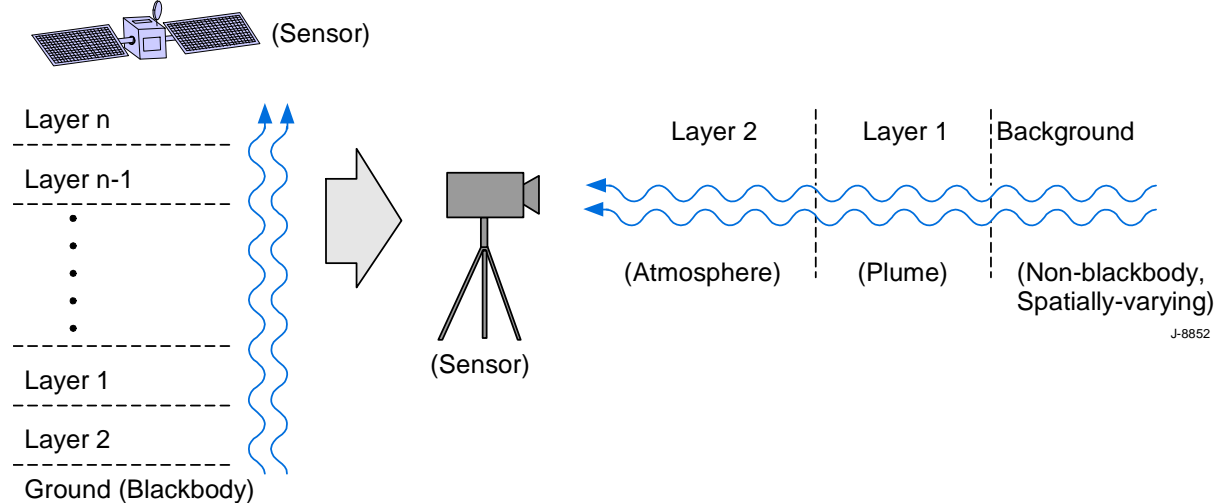
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- Ensemble of measured spectra
- Measured spectra are nonlinear functions of atmospheric temperature, constituent profiles, background characteristics, etc.
- Desire inverse solution to radiative transfer equation (RTE)
- Inverse solution is mathematically ill-posed – no unique solution for  $R_n$

# Relation to Atmospheric Profile Retrieval

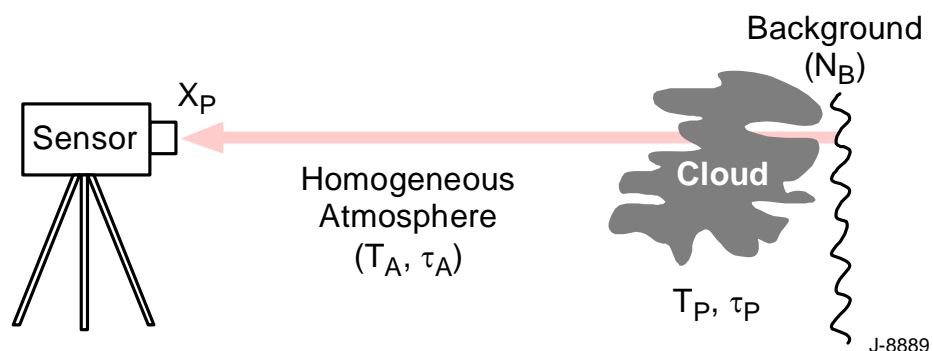
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- **Stratified atmosphere model**
- **Profile retrieval**
  - Many stratifications
  - Simple background
  - Apply constraints to layer-to-layer variation
- **Plume detection**
  - Simple atmosphere
  - Complicated background
  - Apply constraints to background characterization

# Simplified Radiative Transfer Model

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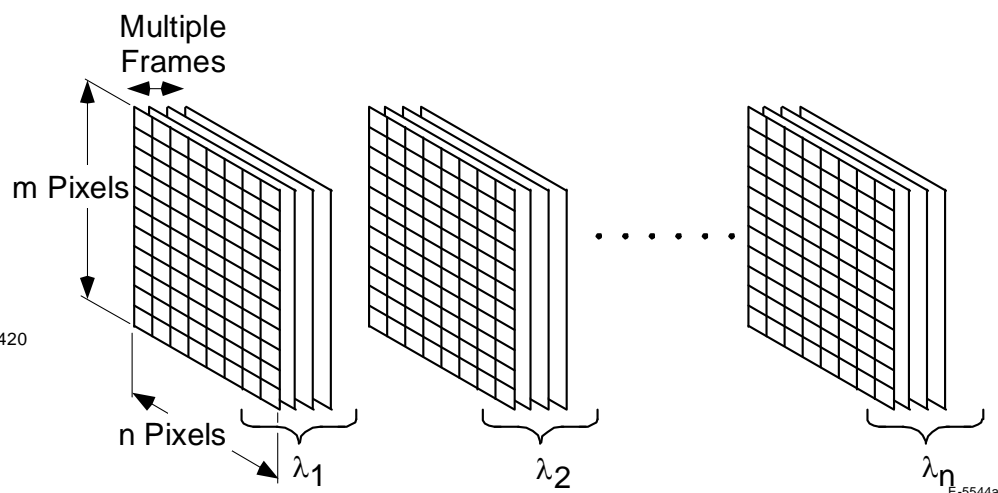
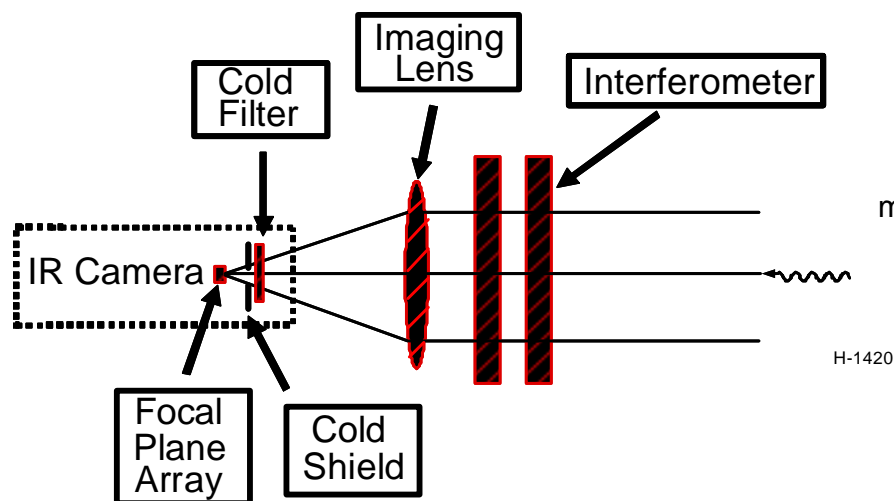
$$x_p = x_0 + (1 - \tau_p) \cdot [(L_a - x_0) + \tau_a \cdot (L_p - L_a)]$$

	Linear (approx.)	Non-Linear (exact)
Plume transmission ( $\tau_p$ )	$1 - \alpha_s$	$\exp(-\alpha_s)$
Radiance contrast ( $L_a - x_0$ )	$\propto \Delta T_{\text{eff}}$	any
Plume temperature ( $T_p$ )	$T_p = T_a$	$T_p = T_a$
Atmospheric scattering	No	No

- **Simplifying assumptions:**
  - Homogeneous atmosphere between sensor and vapor cloud
  - Cloud is at air temperature
- **Compare performance of non-linear (exact) RT model with linearized approximation**

# Adaptive InfraRed Imaging Spectroradiometer (AIRIS)

VG10-076-6



- **Imaging Fabry-Perot spectrometer**

- Mirror spacing  $\sim \lambda$
- Staring IR FPA
- Band sequential data acquisition
- Co-registration of narrowband images
- Tune time  $\sim 2$  ms

- **Selective sampling of wavelengths**

- Acquire imagery only at wavelengths which facilitate target ID
- Minimize data volume

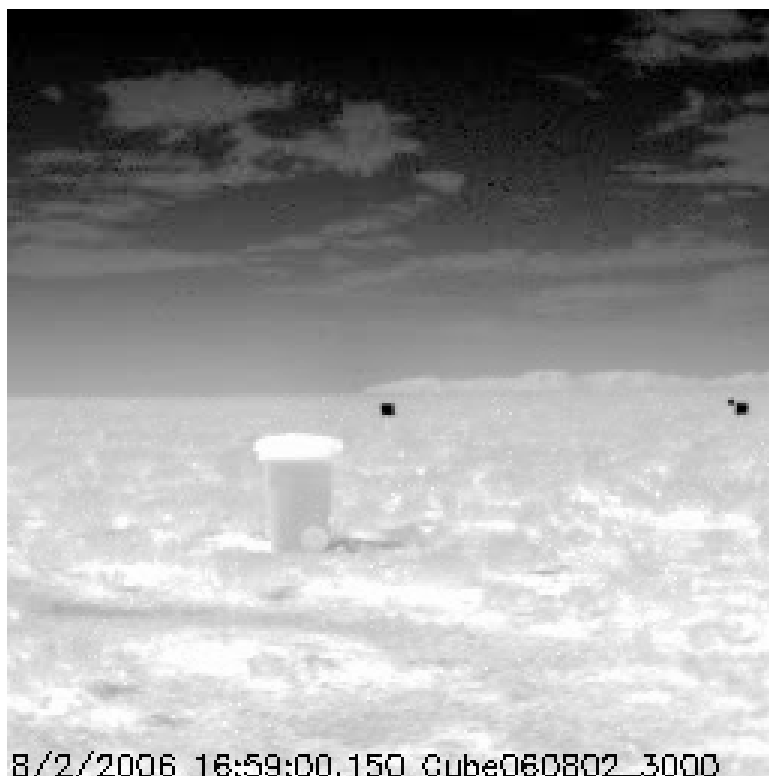
- **Wide field-of-view, wide spectral coverage**



# TEP Detection:

## Shortcoming of Thin Plume Approximation

VG10-076-7



- **Triethyl phosphate (TEP) release**
- **Post-processing:**
  - Non-linear estimator in IDL
  - False alarm mitigation: 4 of 8 spatial filter
  - Bad pixels substituted
- **Detection key:**
  - TEP only
  - Yellow:  $OD \sim 0$
  - Red:  $OD \geq 1$

# Agenda

VG10-076-8

- Introduction
- ***Nonlinear estimation***
  - *Algorithm formulation*
  - Test data
  - Results
- Conclusions

# Optimal Estimation: Bayesian Approach

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- **Bayesian posterior pdf for model parameter values:**

$$p(\theta|\tilde{x}) = \frac{p(\tilde{x}|\theta)p(\theta)}{p(\tilde{x})}$$

- **Maximum likelihood parameter values maximize posterior:**

$$\begin{aligned}\hat{\theta} &= \arg \max \{p(\theta|\tilde{x})\} \\ &= \arg \min \{-\ln p(\theta|\tilde{x})\}\end{aligned}$$

- **Multi-variate normal pdf for deviation between model and measurement:**

$$-\ln p(\tilde{x}|\theta) = \frac{1}{2} [\tilde{x} - f(\theta)]^T D^{-1} [\tilde{x} - f(\theta)] + c_{x|\theta}$$

$$D = \text{diag} \{[\sigma_1^2, \sigma_2^2, \dots, \sigma_k^2]\}$$

- **Prior pdf for model parameter values**

$$-\ln p(\theta) = \frac{1}{2} [\theta - \theta_a]^T R [\theta - \theta_a] + c_\theta$$

# Optimal Estimation: Signal Model

- Signal model:**

$$f(\theta) = \tau_e \circ x_0 + [1 - \tau_e] \circ L_a$$

Diagram illustrating the signal model equation  $f(\theta) = \tau_e \circ x_0 + [1 - \tau_e] \circ L_a$  with components labeled below:

- $f(\theta)$ : calculated spectrum (red arrow)
- $\tau_e$ : calculated plume trans. (blue arrow)
- $x_0$ : estimated "baseline" (green arrow)
- $L_a$ : Blackbody at  $T_{\text{atm}}$  (red arrow)

- Plume transmission:**

$$\tau_e = \exp[-\alpha s]$$

Diagram illustrating the plume transmission equation  $\tau_e = \exp[-\alpha s]$  with components labeled below:

- $\alpha$ : peak OD (red arrow)
- $s$ : reference spectrum (blue arrow)

- Infrared background:**

- Linear mixing model
- Probabilistic Principal Components
- Robust estimate of sample covariance (Huber-type M-estimator)

$$x_0 = \mu + B\beta$$

- Model parameters:**

- $\alpha$ : Plume OD
- $T_a$ : Plume/air temperature
- $\beta$ : Parameters which account for bkgd. radiance given bkgd. model

$$\theta = [\alpha, T_a, \beta]$$

# Minimize Cost Function

- Maximum likelihood parameter values minimize cost function
- Multivariate normal pdfs result in "quadratic" cost function

$$C = [\tilde{x} - f(\theta)]^T D^{-1} [\tilde{x} - f(\theta)] + [\theta - \theta_a]^T R_\theta [\theta - \theta_a]$$

deviation between measured and model spectra

deviation of parameters from nominal values

– Quadratic formulation:  $C = r^T r$

– Prior applied to background coefficients only:  $[\theta - \theta_a]^T R_\theta [\theta - \theta_a] = \beta^T \beta$

– Residuals vector:  $r \equiv [D^{-1/2} [\tilde{x} - f(\theta)]; \beta]$

- Determine maximum likelihood parameter values by nonlinear estimation
  - Approach not limited to quadratic cost function
  - Quadratic cost function amenable to computationally-efficient solution

# Nonlinear Optimization Algorithms

VG10-076-12

- Iterative determination of parameters, e.g., Newton's Method:

$$\theta_{i+1} = \theta_i - \mathbf{H}_i^{-1} (\nabla C)_i$$

Diagram illustrating the Newton's Method update equation for model parameters  $\theta$ . The equation is  $\theta_{i+1} = \theta_i - \mathbf{H}_i^{-1} (\nabla C)_i$ . Annotations include:

- Model parameters** (red arrow) pointing to  $\theta_{i+1}$ .
- iteration no.** (blue arrow) pointing to  $i$  in  $\theta_i$ .
- Hessian matrix** (red arrow) pointing to  $\mathbf{H}_i$ .
- gradient vector** (blue arrow) pointing to  $(\nabla C)_i$ .
- cost function** (green arrow) pointing to  $C$ .

- Gauss-Newton algorithm

– Approximate Hessian matrix:  $\mathbf{H} \approx 2\mathbf{J}^T \mathbf{J}$

– Parameter update equation:  $\theta_{i+1} = \theta_i - (\mathbf{J}_i^T \mathbf{J}_i)^{-1} \mathbf{J}_i^T \mathbf{r}_i$

– Initial guess at  $\theta$  from linear model

- Levenberg-Marquardt algorithm also applicable

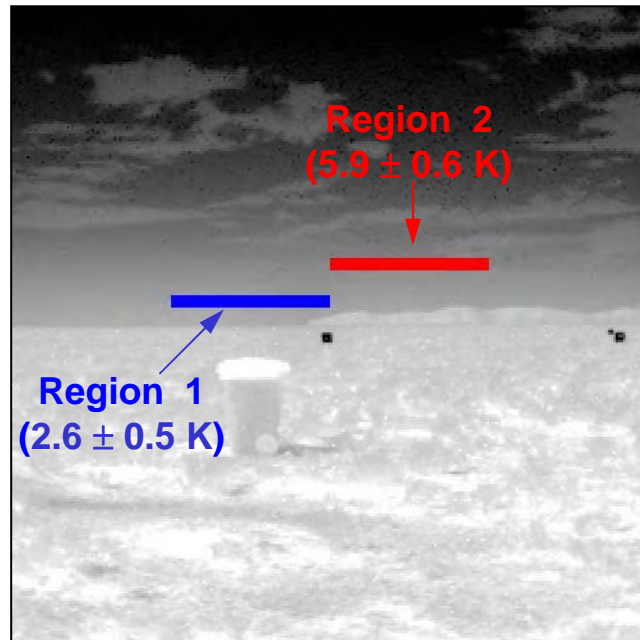
# Agenda

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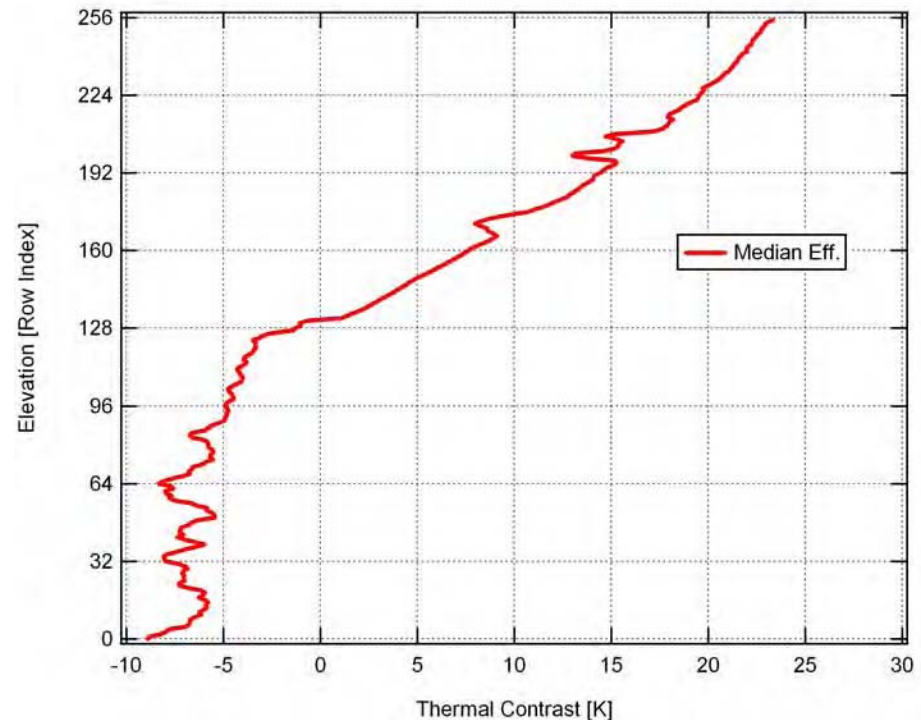
- Introduction
- ***Nonlinear estimation***
  - Algorithm formulation
  - ***Test data***
  - Results
- Conclusions
- Next generation algorithm(s)

# Test Regions

VG10-076-14



AIRIS-WAD datacube: 256 x 256 pixels



- **Plume-free data augmented with synthetic plumes:**

- 64 x 5 pixels
- Max OD from 0 to 3.0 (base e)
- $T(\text{plume}) = T(\text{air}) = 25.0 \text{ deg C}$

- **Thermal contrast**

- ~0 K along horizon
- Monotonic increase with elev. angle

- **Test both favorable and unfavorable regions**



# Simulation: Synthetic R-134a Plumes

VG10-076-15

- **Effective plume transmission:**

- Reference spectrum from PNNL library

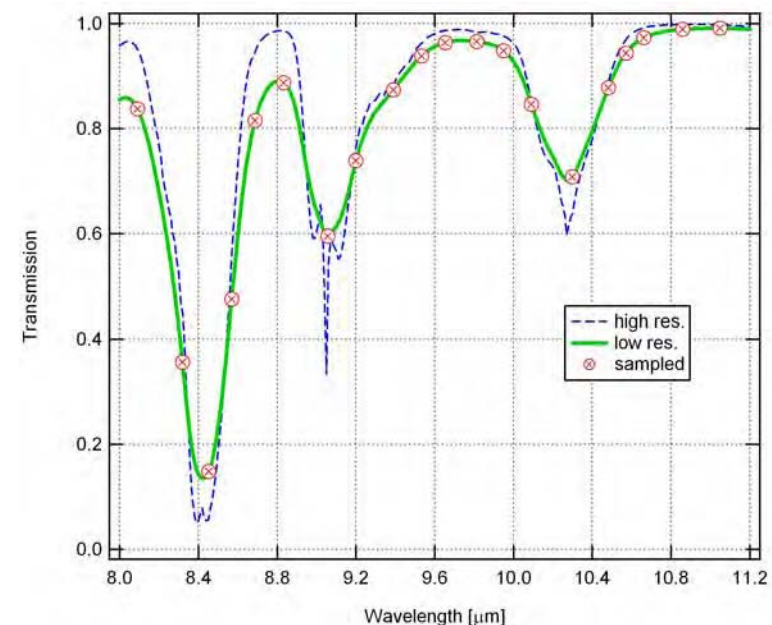
$$\tau(\lambda) = \exp[-CL \cdot \sigma(\lambda)]$$

- Specify column density
- Beer's Law + instrument resolution function

- **Data augmentation:**

- Partition measurement into estimated signal, noise
- Modify signal w/plume signature
- Add back estimated noise

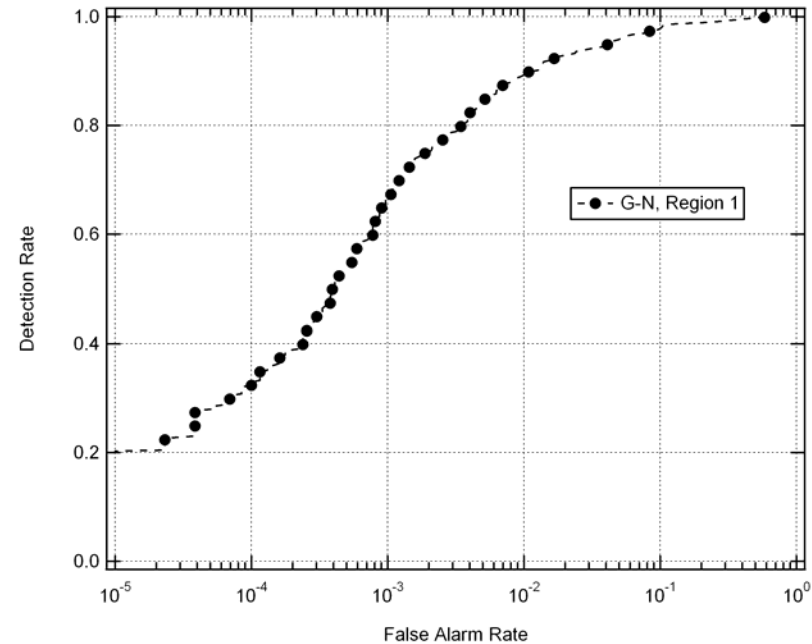
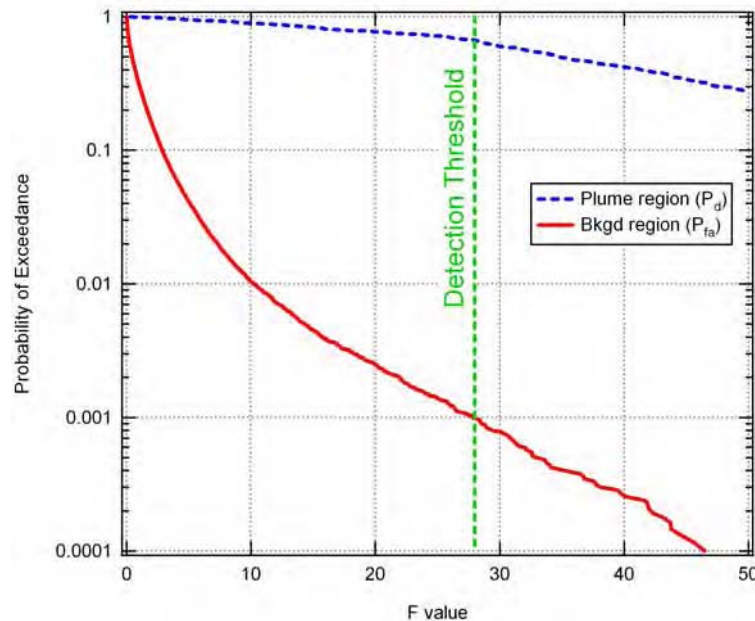
$$x_p = \hat{x}_0 + [1 - \tau_p] \circ [L_a - \hat{x}_0] + \hat{e}$$



$$\bar{\tau}_p(\lambda_s) = \int \tau(\lambda) \cdot g(\lambda, \lambda_s) \cdot d\lambda$$

# Performance Metric: ROC Curves

VG10-076-16



- **Binary decision hypotheses**
  - $H_0$  ("plume absent") and  $H_1$  ("plume present")
  - pdfs for detection statistic:  $p(F | H_i)$
- **ROC curve is  $P_d(F_{th})$  vs  $P_{fa}(F_{th})$** 
  - $P_d$  from plume-augmented region
  - $P_{fa}$  from rest of scene
- **ROC "surface":  $P_d(\alpha; F_{th})$**

$$P_{fa}(F_{th}) = \int_{F_{th}}^{\infty} p(F | H_0) d\eta$$

$$P_d(F_{th}) = \int_{F_{th}}^{\infty} p(F | H_1) d\eta$$

# Agenda

VG10-076-17

- Introduction
- ***Nonlinear estimation***
  - Algorithm formulation
  - Test data
  - ***Results***
- Conclusions

# Performance Comparison with Matched Filter

- **Objective: Compare nonlinear estimation with matched filter estimation**
  - Detection statistics
  - Column density/optical density
- **Detection with nonlinear estimator: F test**

$$F(\tilde{x}) = (k-1) \cdot \left[ \frac{C(\tilde{x}, \hat{\theta}_0)}{C(\tilde{x}, \hat{\theta})} - 1 \right]$$

- **Analogous metric for clutter-matched filter: Adaptive Cosine Estimator (ACE)**

$$D_{MF}(\tilde{x}) = \frac{(s'^T \hat{\Sigma}^{-1} [\tilde{x} - \mu])^2}{(s'^T \hat{\Sigma}^{-1} s')([\tilde{x} - \mu]^T \hat{\Sigma}^{-1} [\tilde{x} - \mu])}$$

$$F_{MF} = (k-1) \frac{D_{MF}}{1 - D_{MF}}$$

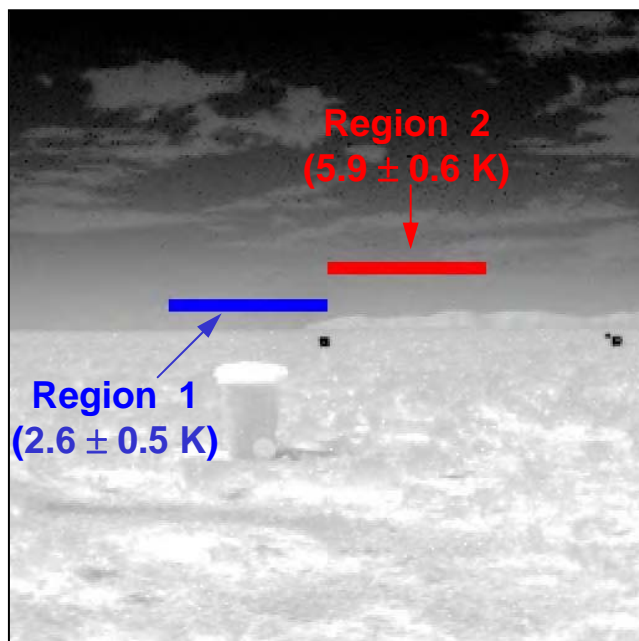
- **Matched-filter optical density estimate:**

$$\hat{\alpha}_{MF} = \frac{s'^T \hat{\Sigma}^{-1} (\tilde{x} - \mu)}{s'^T \hat{\Sigma}^{-1} s'} \cdot \frac{\Delta T_0}{\Delta T_{eff}}$$

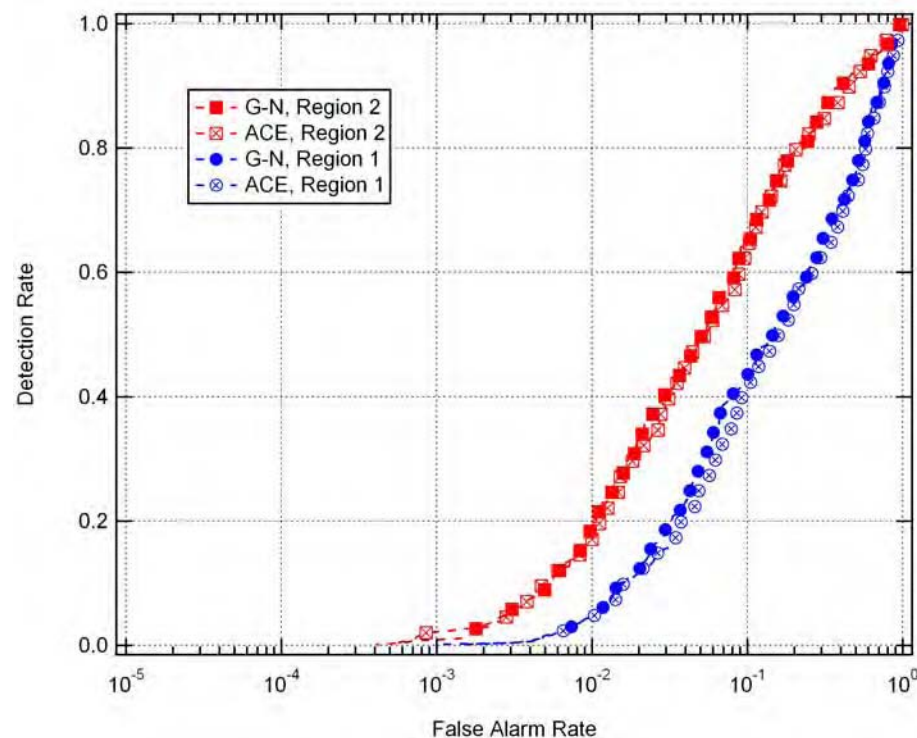
- ***Expect near identical results for optically-thin plumes***

# R-134a Detection: Optically-Thin Plume, OD=0.1

VG10-076-19



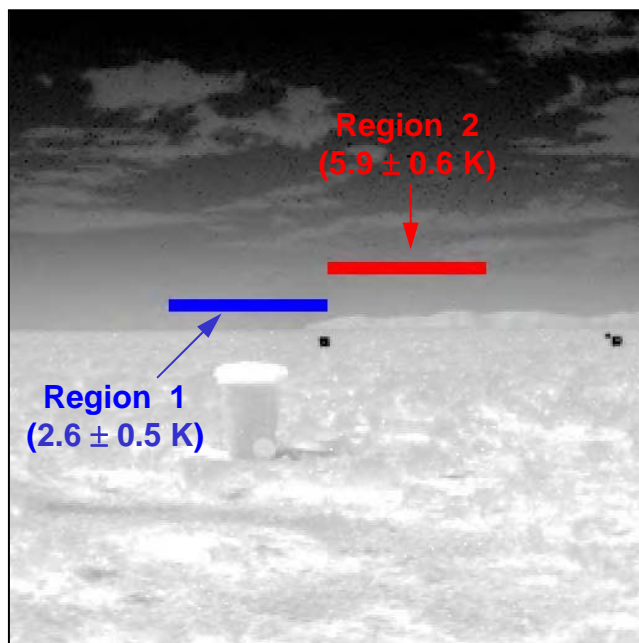
AIRIS-WAD datacube: 256 x 256 pixels



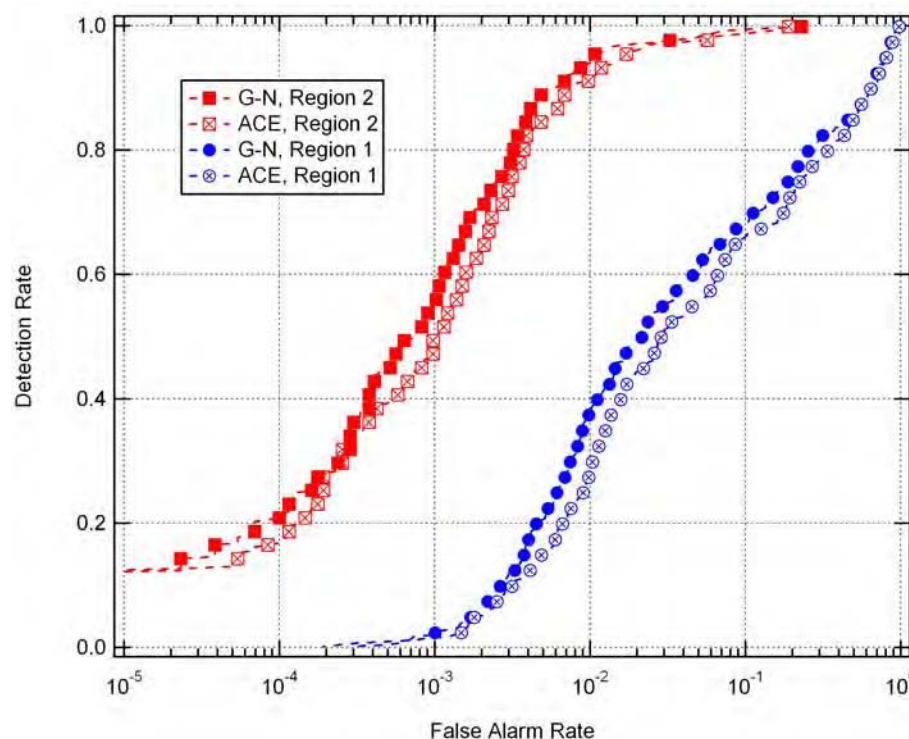
- Plume column density = 82 mg/m<sup>2</sup> (20 ppmv-m)
- Detection statistics not favorable in either Region
- ACE and Gauss-Newton ROC curves are nearly identical
  - 20 bands in test datacube
  - OD=0 reference spectrum

# R-134a Detection: Optically-Thin Plume, OD=0.3

VG10-076-20



AIRIS-WAD datacube: 256 x 256 pixels



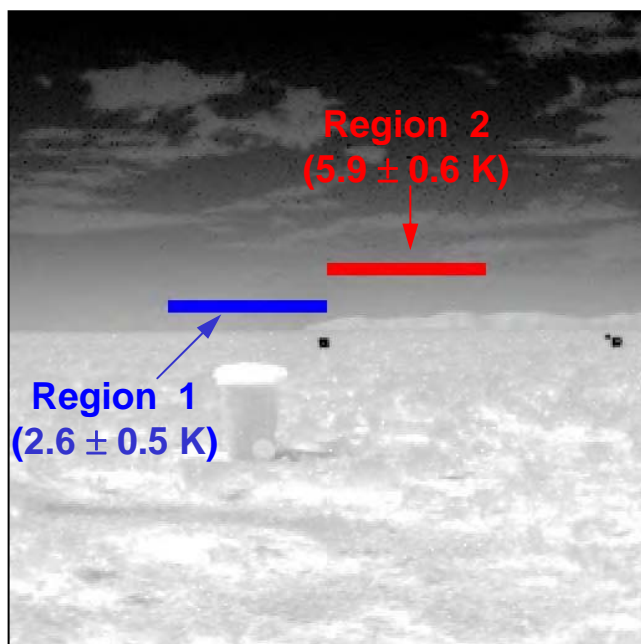
- Plume column density = 246 mg/m<sup>2</sup> (59 ppmv-m)
- Detection statistics not favorable in Region 1, marginal in Region 2
  - Lower thermal contrast
  - ~2 orders of magnitude reduction in  $P_{fa}$  from Region 1 to Region 2
- ACE and Gauss-Newton ROC curves are nearly identical



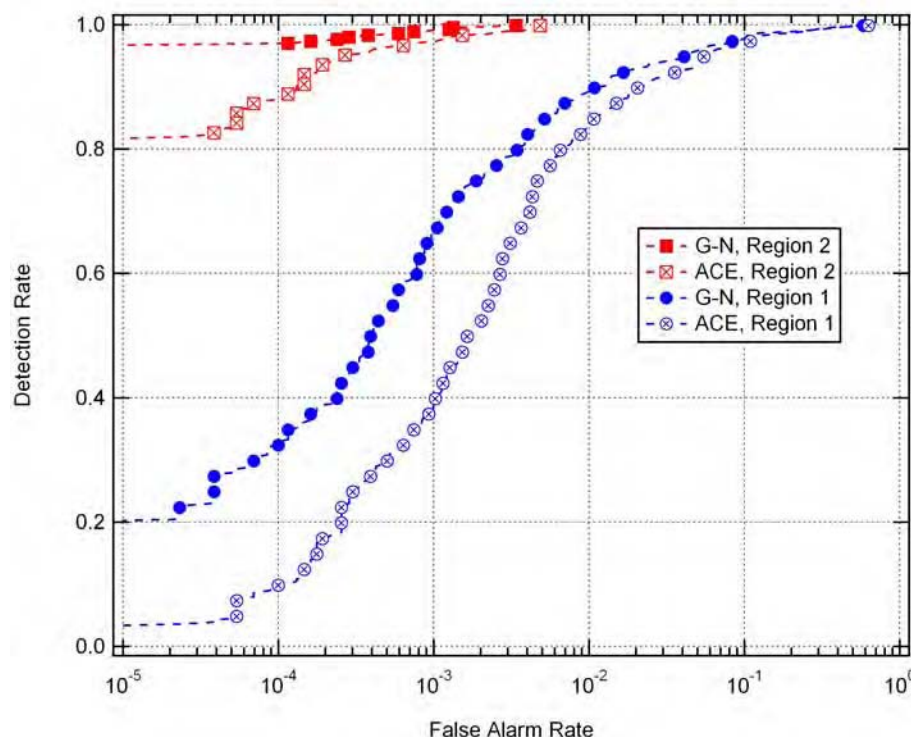
# R-134a Detection: Optically-Thick Plume, OD=1.0

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VG10-076-21



AIRIS-WAD datacube: 256 x 256 pixels

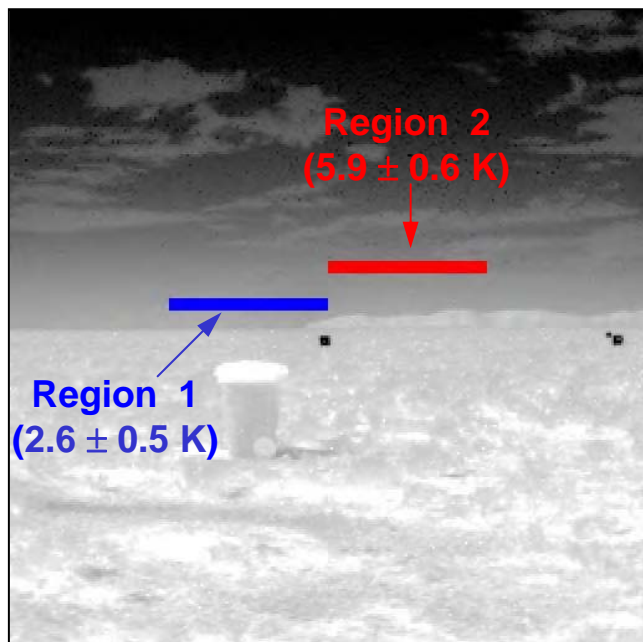


- **Plume column density = 822 mg/m<sup>2</sup> (197 ppmv-m)**
- **Detection statistics favorable in Region 2, marginal in Region 1**
  - >2 orders of magnitude reduction in  $P_{fa}$  from Region 1 to Region 2
- **Gauss-Newton produces significantly more favorable ROC curves than ACE**
  - Factor of ~2 improvement in Region 1 ( $P_{fa}$  for fixed  $P_d$ )
  - Multiple orders of magnitude improvement in Region 2

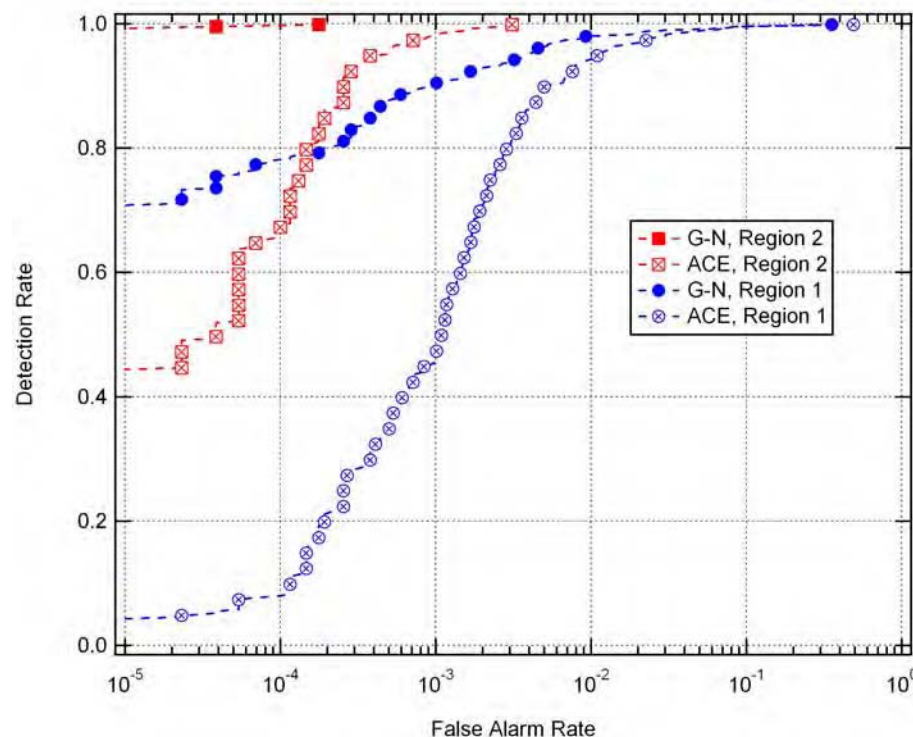
# R-134a Detection: Optically-Thick Plume, OD=2.0

Physical Sciences Inc.

VG10-076-22



AIRIS-WAD datacube: 256 x 256 pixels

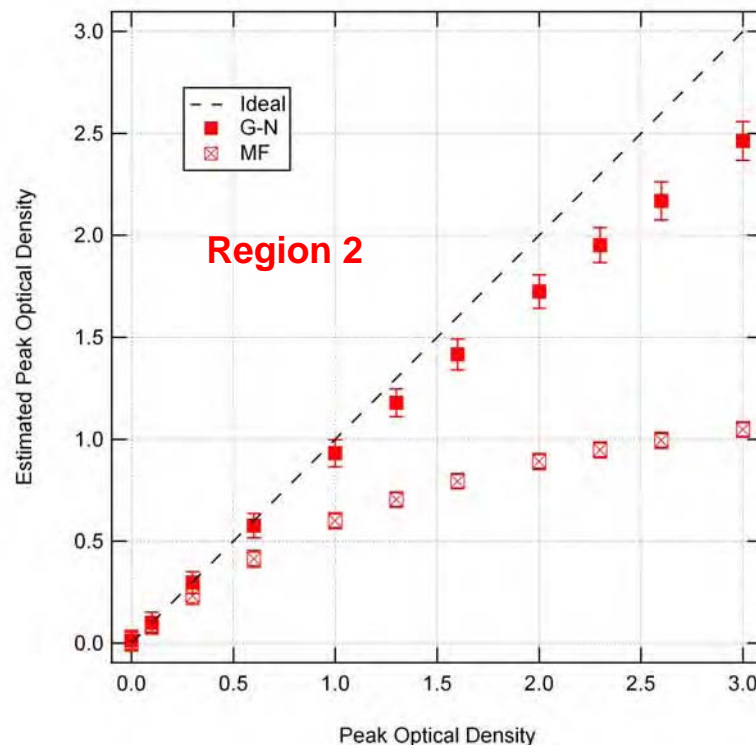
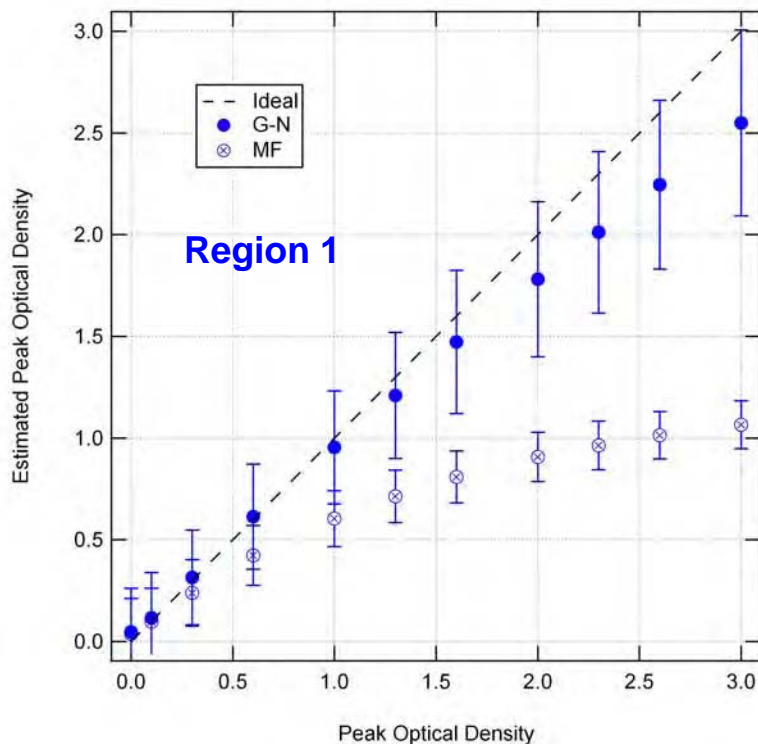


- Plume column density = 1643 mg/m<sup>2</sup> (394 ppmv-m)
- Detection statistics favorable in both Regions
- Gauss-Newton produces significantly more favorable ROC curves than ACE
  - >1 order of magnitude improvement in Region 1
  - Multiple orders of magnitude improvement in Region 2



# Column Density Estimation

I-076-23



- Increased thermal contrast reduces uncertainty, no effect overall accuracy
- Nonlinear estimation
  - Accurately recovers embedded OD (CL)
  - Systematic deviation at OD>1 is instrument resolution effect
- Matched Filter systematically underestimates CL
- *Nonlinear estimator always as good or better than MF*

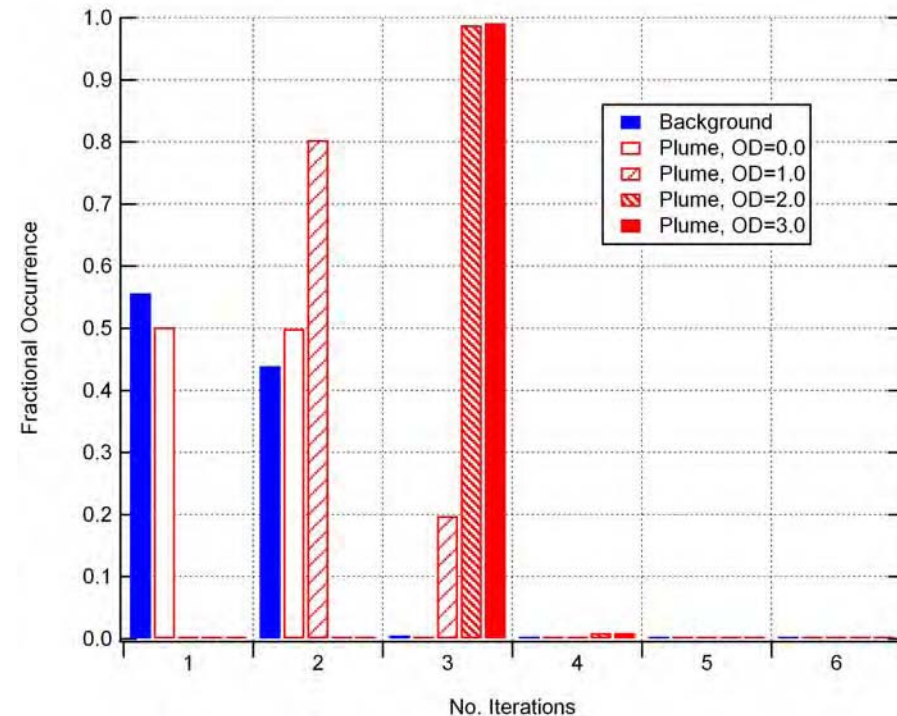
# Algorithm Execution

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- Gauss-Newton algorithm is iterative
- Termination criterion:

$$0 < \left[ 1 - \frac{C_{i+1}}{C_i} \right] < \delta_{\max}$$

- Initial guess is Iteration 0
- Typical results:
  - 1-2 iterations for no plume (plume OD=0)
  - 3 iterations to converge for OD~2-3 TEP plume
- Decreasing  $\delta$  to 0.0001 increase no. iteration but no statistically-significant effect on CL



$$\delta_{\max} = 0.01$$

# Summary and Conclusions

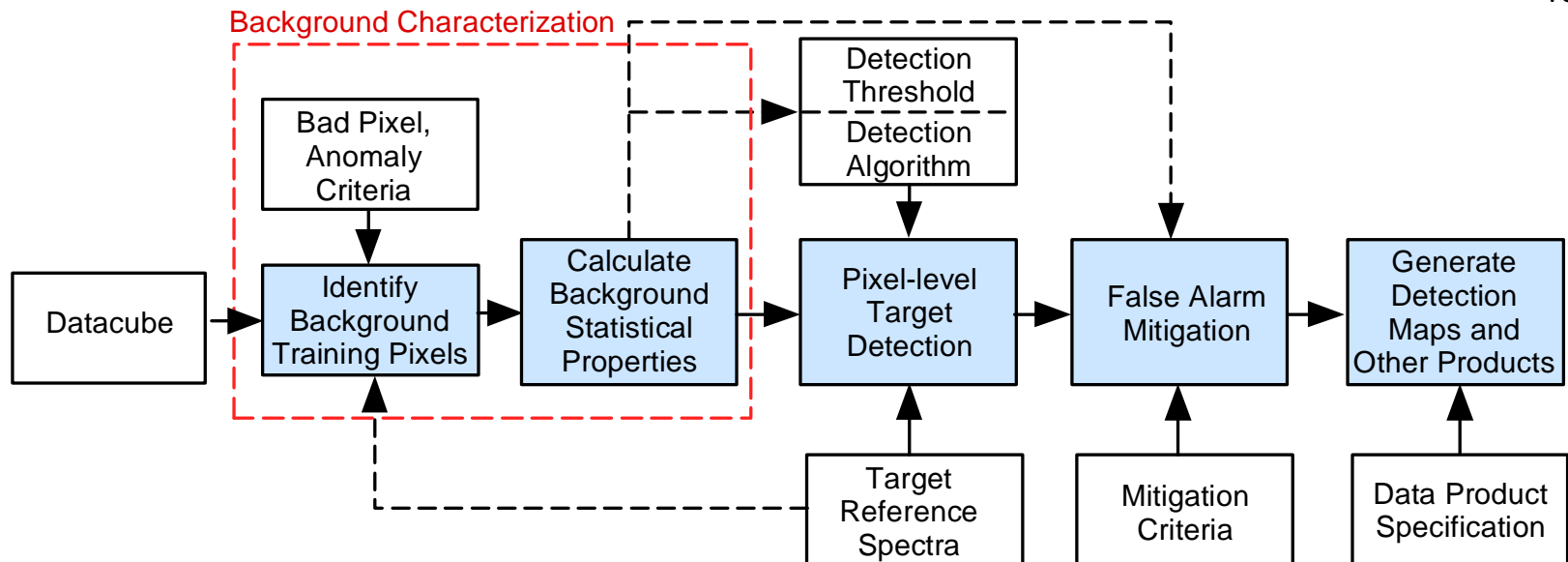
VG10-076-25

- **Developed nonlinear estimator for plume detection and characterization based on RTE**
  - Bayesian formulation
  - Statistical model for IR background
  - Gauss-Newton algorithm to estimate maximum *a posteriori* (MAP) values
- **Signal model developed for non-scattering atmosphere, single layer plume**
  - Easily modified to address more complicated atmospheres
- **Nonlinear estimation significantly outperforms matched-filter-based with optically-thick plumes**
  - "Orders of magnitude" improvement
  - NL estimator and matched filter produce equivalent results for optically-thin plumes
- **This work was performed under Contracts from the Defense Threat Reduction Agency (HDTRA01-07-C-0067) and US Army ECBC Aberdeen Proving Ground, MD (W911SR-06-C-0022). Any opinions, findings and conclusions or recommendations expressed in this material are those of the author and do not necessarily reflect the views of HDRA or the Army.**

# **Additional Material**

# Data Processing Chain

VG10-076-27



J-6549a

- **Focus is pixel-level target detection**
- **New background characterization approach facilitates improved pixel-level detection**
- **"A chain is only as strong as its weakest link."**
  - Provide higher quality input to False Alarm Mitigation block
  - False Alarm Mitigation is separate issue

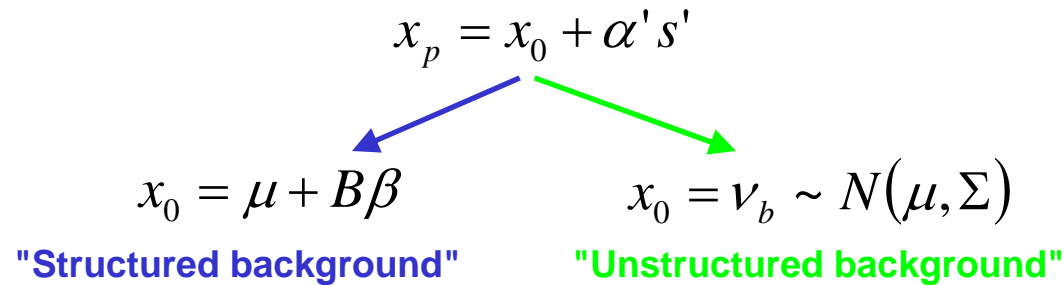
# Technical Approach

VG10-076-28

- **Adapt methodology used for atmospheric profile retrieval from space-based sensor data (e.g. AIRS, IASI, MODIS, TES)**
  - Parameterize Radiative Transfer Equation (RTE)
  - Apply Estimation Theory to determine max. likelihood parameter values
  - Exploit large data set: utilize ensemble statistics
- **Rationale:**
  - Physics-based model for observations
  - Statistically-justified constraints
  - Strong theoretical foundation (see, e.g., C.D.Rodgers, Inverse Methods for Atmospheric Sounding)
- **Benefits**
  - Adaptable framework
  - Immediate application to non-scattering atmosphere
  - Can modify RTE to address more complicated atmospheres

# Linear Models

VG10-076-29



- **"Structured Background"**

- Values of  $\beta$  are unconstrained
- Generalized Likelihood Ratio Test:

$$D_{GLRT}(x) = \frac{x^T P_B^\perp x}{x^T P_{SB}^\perp x}$$

$$P_B^\perp = I - B(B^T B)^{-1} B^T$$

- Typical implementation:  $B$  = eigenvectors of sample covariance matrix

- **"Unstructured Background"**

- $v_b$  is a random vector
- Adaptive Cosine Estimator:

$$D_{ACE}(x) = \frac{[s'^T \Sigma^{-1} x]^2}{[s'^T \Sigma^{-1} s'] [x^T \Sigma^{-1} x]}$$

- **Survey article: Manolakis, Marden, & Shaw, "Hyperspectral Image Processing for ATR Applications," *Lincoln Lab J.*, v.14 (2003)**

# Pros and Cons of Linear Approximation

VG10-076-30

- **Pro: Matrix multiplication results in fast computation**
  - All spectra in ensemble may be processed in parallel
  - Major computational expense is diagonalization of sample covariance matrix
  - *AIRIS-WAD: <150 ms to process 65536 twenty element spectra for four target signatures (using 2005 vintage technology)*
- **Pro: Detection statistics well-understood for Gaussian noise**
- **Con: Underlying physical assumptions not valid for detection scenarios of interest**
  - Mathematical model not matched to physics

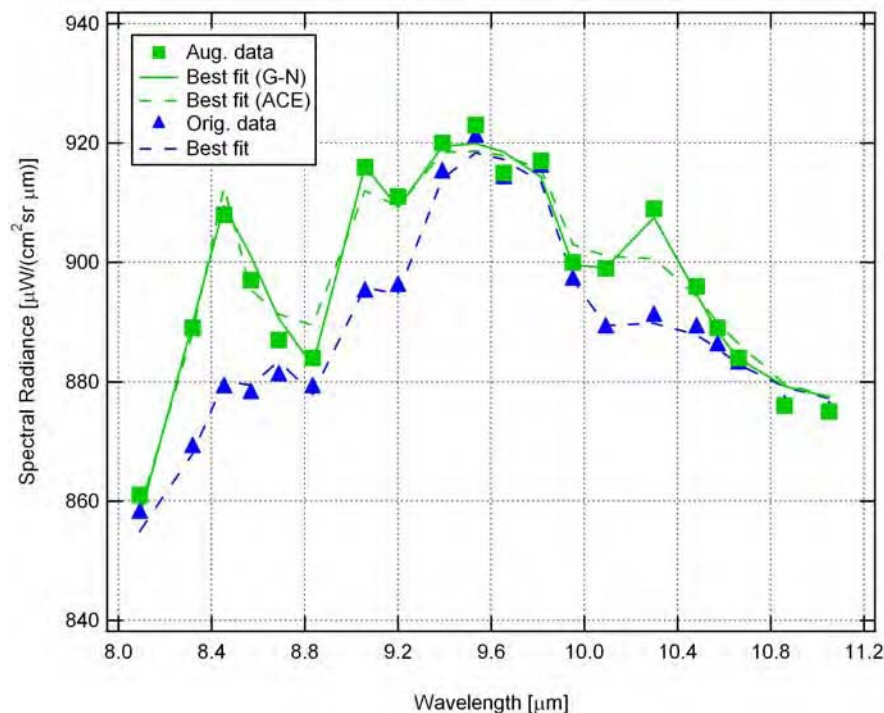
$$\tau_p = \exp(-\alpha s) \approx 1 - \alpha s$$

- Linear approximation to Beer's Law can introduce significant error

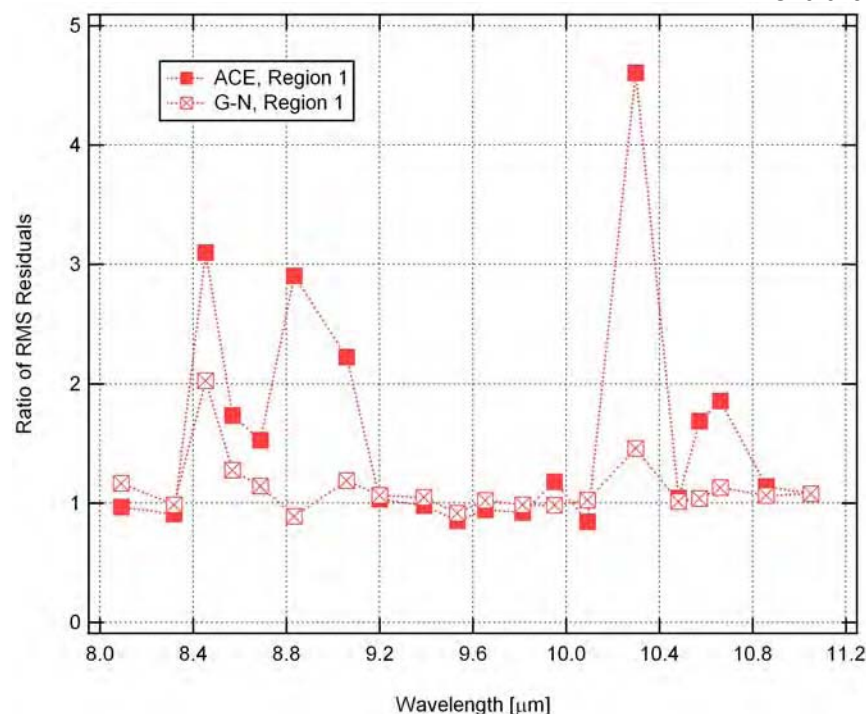


# Why Gauss-Newton Yields Better Results

VG10-076-31



Spectrum augmented with OD=3.0 plume



Ratios of rms residuals in plume region, OD=3.0 to OD=0

- **Model is matched to the data**
- **Fit residuals are systematically larger with linear model**
  - Result of least-squares minimization
  - Location of largest residuals highly correlated with strongest R-134a absorption features

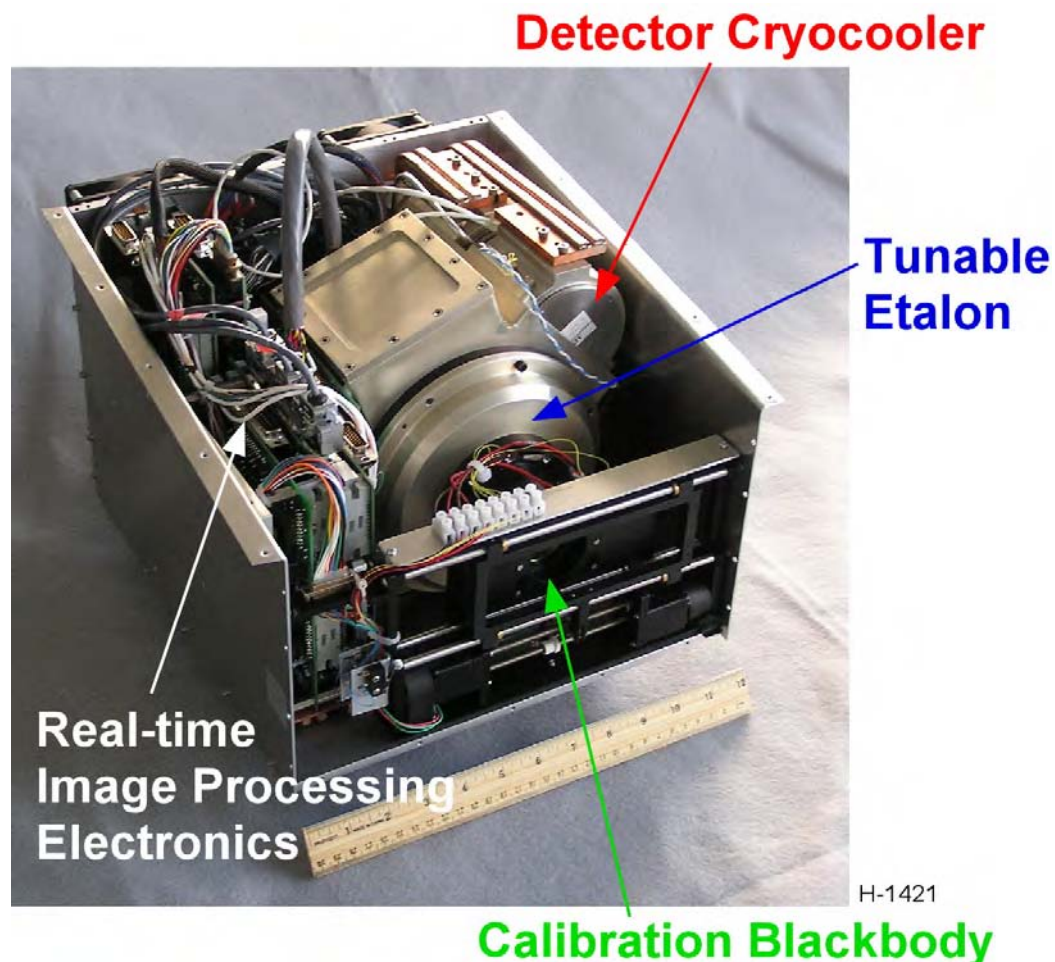


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# Adaptive Infrared Imaging Spectroradiometer – Wide Area Detector (AIRIS-WAD)

VG10-076-32

- **Optical:**
  - 256 x 256 pixels
  - 30 deg x 30 deg FOV
  - spectral coverage: 7.9 to 11.2  $\mu\text{m}$  at  $\sim 0.1 \mu\text{m}$  resolution ( $\sim 1\%$  of  $\lambda$ )
- **Datacubes:**
  - 20 wavelengths
  - user selectable  $\lambda$ 's, specified prior to mission
- ***Real-time datacube processing: up to 3 Hz***
- **Detection algorithm history:**
  - GLRT: Winter 2005-Spring 2006
  - ACE: since Spring 2006



H-1421

# Hyperspectral Background Model

VG10-076-33

- **Probabilistic Principal Components-based**

- M.E.Tipping & C.M.Bishop, *J.R.Statist. Soc. B* (1999)

- **Linear mixing model**

$$x = \mu + B\beta$$

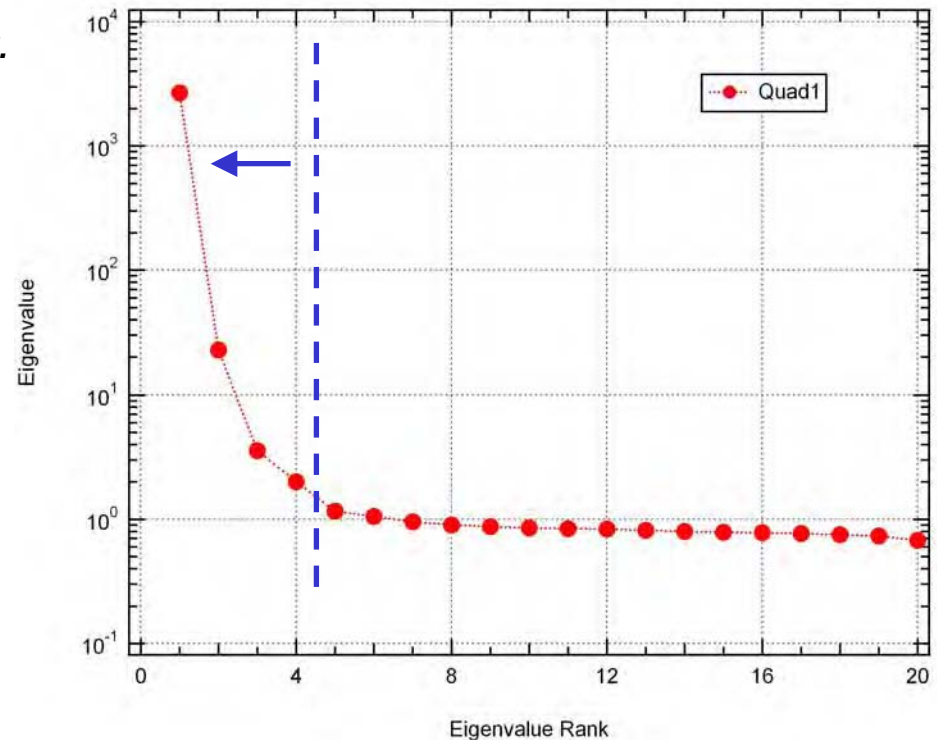
- **Eigenvalue-based covariance regularization**

$$\Sigma \approx \hat{\Sigma} = BB^T + \varepsilon D$$

$$\Sigma = D^{1/2}(U\Lambda U^T)D^{1/2}$$

$$B = D^{1/2}U_m(\Lambda_m - \varepsilon I_m)^{1/2}$$

- **$\Sigma$  = robust estimate of sample covariance: Huber-type M-estimator**



# Gauss-Newton Algorithm

- Follows from Newton's method – simplifying approximations
- Good for solving weakly nonlinear equations
- Hessian matrix:

$$H_{jk} = 2 \sum_{q=1}^m \left[ \frac{\partial r_q}{\partial \theta_j} \frac{\partial r_q}{\partial \theta_k} + r_q \frac{\partial^2 r_q}{\partial \theta_j \partial \theta_k} \right]$$

$$\approx 2 \sum_{q=1}^m \left[ \frac{\partial r_q}{\partial \theta_j} \frac{\partial r_q}{\partial \theta_k} \right] = 2 J^T J$$

$$J = \frac{\partial r}{\partial \theta} \leftarrow \text{Jacobian}$$

- Gradient:  $[\nabla_{\theta} C]_j = \frac{\partial C}{\partial \theta_j} = 2 \sum_{q=1}^m \left[ r_q \frac{\partial r_q}{\partial \theta_j} \right]$

$$\nabla_{\theta} C = 2 J^T r$$

- Parameter update equation:

$$\theta_{i+1} = \theta_i - (J_i^T J_i)^{-1} J_i^T r_i$$

- Initial guess at  $\theta$  from linear model